$\angle O L D E N$ RULE MATH


Dr. Del's

# Golden Rule 

## Math

for

## Struggling Math Students

$21^{\text {st }}$ Century Technologies and Tools
Revolutionizes and Transforms
$21{ }^{\text {st }}$ Century Math Education
for All of Our Wonderful
$21^{\text {st }}$ Century Math Students

Delbert Craig Hane, Ph.D. (Math) aka Dr. Del Founder and CEO, Triad Math, Inc.

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## Table of Contents

Introduction - A Typical Homeschool Story ..... 1
Chapter 1: Math? Help! ..... 3
Chapter 2: Proper Content ..... 7
Chapter 3: SPIKE Pedagogy ..... 11
Self-pacing ..... 11
Proper Content ..... 12
Interactivity ..... 13
Keeping Score ..... 14
Empathy and Humor ..... 15
Chapter 4: Teacher \& Coach ..... 19
Chapter 5: How to Be a Great Coach ..... 23
Chapter 6: Grace's Story ..... 29
Chapter 7: Craig's Story. ..... 35
Chapter 8: Future Math Possibilities ..... 45
Getting Started. Tier 1 and the Scientific Calculator ..... 45
Foundation - Practical Math. Tier 2 ..... 46
College-Bound SAT or ACT Prep. Tier 3 ..... 47
STEM Math PreCalculus. Tier 4 ..... 48
Calculus the right 21 st Century way. Tier 5 ..... 49
Differential Equations. Tier 6 ..... 51
Free Resources ..... 53
Special Offers ..... 55
Affiliates ..... 57
Who is Dr. Del? ..... 59

## Introduction A Typical Homeschool Story

A frantic call came in to Dr. Del from Ruth, a homeschool parent.
"Dr. Del, I'm a homeschool parent with a child, Jacob, age 12, who is struggling with math.
"I have been able to teach him some basic elementary math.
"But, I am way over my head going forward.
"We have used several different math programs, and frankly, nothing is working for him.
"Can you help me?" asked Ruth.
"Yes, I believe so, but first a question. OK?" answered Dr. Del
"OK.." said Ruth.
"Can Jacob play any games of any kind, or work on puzzles of any kind, or build things, or play a sport, or do anything that requires some skills?" asked Dr. Del.
"Oh yes, he's pretty good at playing various games, and he loves to play them." said Ruth.
"Good news then. Jacob can learn math. Math should be treated like a game or sport." said Dr. Del
"Really?" replied Ruth.
"Oh, YES! Really!" said Dr. Del.
"This book will show you how and why this is the case, and most importantly, how you can cause it to happen.
"I'll be the Teacher and you'll be the Coach, and Jacob will enjoy and succeed in learning math.
"The 'Secrets' are SPIKE Pedagogy and Proper Content".
"That's what you will learn in this book." said Dr. Del.
"Wow, that's wonderful. Thanks so much!" exclaimed Ruth.
"We'll both know how Jacob is doing as you will learn." said Dr. Del.
"Keep up the good work and on to success for Jacob!"
Dr. Del has had similar conversations and experiences with many other students.

See Grace Libman's story in Chapter 6 and Craig's own story in Chapter 7.

Then, be sure to take advantage of one of the Special Offers to begin to help your own struggling math student.

Also, if you have a successful math student, especially a potential STEM student, be sure to read one of the other Golden Rule Math books aimed at those students, too.

## Chapter 1: Math? Help!

This chapter is for a parent with a child who is struggling with math.

For all other students, I recommend the appropriate Golden Rule Math book in this series, perhaps starting with the $21^{\text {st }}$ Century Math Student book.

So, here are two questions a parent might have, and eight questions ta student might have.

The answers to these questions should help both the parent and the child/student.

I will give you the quick answers below.
And then, tell you what to do in the following chapters.
If you want more in depth answers, then there is also a 24 page eBook, Math? Help!, for parents with a child who is struggling with middle or high school level math that I wrote some years ago that gives my answers to these questions in quite a bit of detail. You may get a free PDF copy of it, too.

Go to www.HomeschoolerToday.com, and click the Free Resources Tab. Then, click on the Educational Tab at the top, and then select eBooks. Now, you can download the Math? Help! eBook in PDF format.

I suggest you think about what you, the reader, think the answers are for these ten questions for both you and your child.

Then look at my short answers below or in the eBook Math? Help! for a more in depth discussion.

Ultimately, you must come up with answers you believe, and then act on them in the best way you can for your child.

1 and 2 are for parents, and $3-10$ are for the student.

1. Why is my child struggling with math?
2. What can I do about it for my child?
3. What's Math all about?
4. Why is Math hard for me?
5. Is it MY fault or am I "stupid"?
6. How can I understand math?
7. Can math be EASY for me?
8. Can math be FUN for me?
9. What good will Math do ME?
10. So, what should I do, RIGHT NOW?

Following are my very short answers. More details may be found in Math? Help!

## Math? Help!

1. Why is my child struggling with math?

Poor Pedagogy and Improper Content
2. What can I do about it for my child?

Deliver Proper Content (Ch 2) with SPIKE Pedagogy (Ch 3)
3. What's Math all about?

Numbers and Geometry and
Modern TOOLS to solve problems
The Modern TOOLS make learning math much easier too!
4. Why is math hard for me?

See \#1. Your parent can explain.
5. Is it MY fault or am I "stupid"?

NO! Math is no harder than your games you are good at.
6. Can I understand math?

YES! In fact, you can get good at it.
7. Can math be EASY for me?

YES! When taught properly to you.
8. Can math be FUN for me?

YES! Math is a great game.
9. What good will Math do ME?

Math can transform your life.
Math will empower you to pursue many different careers, and learn many things that might interest you either as a hobby or a job.

Math will teach you how to: Learn to Learn
10. So, what should I do, RIGHT NOW?

Read and understand the rest of this book, and then act on a Special Offer and become a Successful Math Student.

## Chapter 2: Proper Content

If you don't understand the decimal number system, have your parent teach it to you following the Uncle Jack videos. [Note to Parent: They will be available to you when you take advantage of Special Offer \#2.]

Once you understand numbers, learn to use the TI-30Xa Scientific Calculator to do your arithmetic calculations and be sure you understand the Rules of Arithmetic.

This is all covered in Tier 1 of Triad Math's Online Program.

Most students find this very easy and fun, and do it in a couple of weeks.

It is self-paced and will take various amounts of time for different students.
[Parent: Pay close attention to the Coaching Principles and Guidelines.]

Now, move on to Tier 2:
First, learn Practical Algebra Tier 210 Lessons
Second, learn Practical Geometry Tier 219 Lessons
Third, learn Practical Trigonometry Tier 27 Lessons
Wow, all of this in only 36 Lessons!

You probably will be able to complete Tier 2 in two or three months if you will work a little most days, say 30 minutes to an hour, five days a week.

Most of your time will be spent doing exercises and reviewing.

You will watch the Tutorial Videos to learn the topics and how to do the exercises.

Then, take a short Quiz to be sure you have mastered the topic.

Your ONLY Grade will be a A.
You then will know more math than most adults in the USA and be ready for the military or technical workforce, or to learn any technical field.

Here is my one question 'test' you will be able to answer that you can use to prove this!

It will impress many of your family and friends.
My one question test, which will prove you are now "Matherate" for the practical technical workforce, is you will be able to calculate, in less than one minute, the area of a triangle with sides of $8.3 \mathrm{in}, 10.4$ in and 15.4 in . Or, any other triangle.

The solution involves most of the things you have now learned, including Practical Trigonometry and the TI30Xa Scientific Calculator. Easy peasy!

Very few people can solve this practical problem!
It's a great way to challenge a "wise guy" with a friendly bet.

## Proper Content

Let them choose the lengths of the three sides of the triangle.

Then find the area!

## Have FUN!

(Answer: 40.5 sq in )

## Immediate Action Plan

Go to HomeschoolerToday.com and enroll your student into the Tier 1 Program and try it out.

Better yet, enroll in the Succeed with Math Crusade and you will have 30 days to see if this program works for your child, and you! No Risk.

See Special Offers below.
The parent can be the coach. See Chapters 4 and 5 .
Dr. Del is the teacher available via the Tutorial Videos and Learning Management System 24/7 for less than $\$ 1$ per day, maybe much less.

You may print out the Tiers 1 and 2 Notes and Exercises PDFs, or you may buy them at Amazon:

Tier 1 Notes and Exercises - https://amzn.to/3ouylMX
Tier 2 Notes and Exercises - https://amzn.to/32PqI6L

Struggling Students

## Chapter 3: SPIKE Pedagogy

Pedagogy means: "The method of teaching a subject"
SPIKE Pedagogy is wonderful for delivering an optimal math education to any student, if you can do it.

Any good math tutor knows this.
SPIKE Pedagogy is practically impossible to practice in a group environment.

Fortunately, parents can easily practice SPIKE Pedagogy for each of their children thanks to a modern $21^{\text {st }}$ Century Math Program.

Any experienced math teacher or tutor will tell you there are five ingredients of good pedagogy for Math expressed by the acronym SPIKE.

So, what is SPIKE Pedagogy? S P I E

Self-pacing. Each student will learn math at his or her own pace which is determined by many factors unique to each student.

It is difficult, usually impossible, for a student to have selfpacing in a group environment where the Math is being taught on a schedule.

Any good math tutor realizes this, and this is one reason why rich parents use good tutors to teach their children math, especially when they are struggling with math taught in a classroom to a group of students.

Indeed, that is how Dr. Del made a good living during his school years from ages $15-27$, high school thru graduate school, and learned the value of SPIKE Pedagogy

Proper Content. A student should be taught Math in a sequence of topics so that the student always has the necessary pre-requisite math knowledge for each new topic.

Furthermore, it is desirable that the Math topics chosen are of interest and relevance to the student.

This is a horrible failure of our current Standard Math Curriculum taught in most Math Programs which include many obsolete manual tools and some premature theory.

An essential ingredient of proper motivation is to explain to the student how a given topic might serve the student well in the future given the student's larger potential interests in life.

Just realize that Math is a HUGE subject.
No single human understands or knows all of the Math there is.

Different people need different math topics depending on their broader interests in life.

Just like any language.

## SPIKE Pedagogy

Indeed, Math is a Universal Language capable of
expressing things no natural language can.
And, Math is Math anywhere in the world.

Interactivity. Math is like a sport or game.
To learn math, you must do (play!) math.
You must practice.
Do lots of math problems.
You will make a lot of mistakes.
You will struggle to overcome hurdles.
Fortunately, with the right attitude Math can be one of the most fun and rewarding sports or games you can ever play.

This is why the psychology of the student is so important.
The student must enjoy the sport or game of Math.
This is why having both a great teacher and a great coach is so important.

The teacher explains the Math and selects the proper topics for the student.

The coach guides and encourages the student.
Mistakes are celebrated as evidence of effort, just like in a sport.

Personal achievements are celebrated as the student climbs the ladder of Math topics.

The coach must be sure the student doesn't miss any rungs of the ladder.

The coach must be sure the student practices.
The coach should point out how Math might help the student in many arenas of the student's future life.

## Keeping Score.

It is very important to keep score of a student's progress and recognize the student's progress and achievements, just like any game or sport.

This is an important responsibility of the coach.
Keeping Score is a powerful motivator for a student.
This is not a grade. It is climbing the Ladder of Topics.
The grade is always an A when a topic is mastered.
It is like ranks and merit badges in scouting.
Or, playing a game with one's self.
Climbing the Ladder of Success.
It is important to create and maintain a good psychology for the student.

Math can sometimes be frustrating for almost any student.

So says Dr. Del.
"I have a Ph.D. in Math, but I can tell you that many times I was frustrated.
"I probably have made more mistakes in Math than anyone you know.
"Remember, Babe Ruth was the Strikeout King, as well as the Home Run King."

## The Proper Math Content will vastly improve most students' lives.

Keeping score will prove this when you compare it to the student's other achievements, especially those that depend on a good Math foundation.

## Empathy and Humor.

A good math student will practice a lot, and make a lot of mistakes.

When I make a mistake, I just chuckle a little, correct it, and go on.

If I make a big mistake I laugh out loud.
Life is funny and fun if you approach it right.
In your life you will make a lot of mistakes.
Indeed, mistakes are a sign of growth.
You learn from your mistakes.
It is up to you to decide how to deal with them.

This is very important if you want to maintain a good healthy psychology.
"I would not have earned a Ph.D. in Math IF I had not learned to laugh at myself and my mistakes," confesses Dr. Del.

## Summary:

OK, SPIKE Pedagogy is necessary for a good Math Education.

The facts are that it is very difficult to deliver the SPIKE Pedagogy for each student in a group setting of many students, which is how math is still being taught in many of our schools.

That is why Homeschool Math can be superior to Public School Math.

In a typical classroom, the teacher will be going too fast for some students and they will fall behind and FAIL.

Any grade less than an A is essentially failure.

## You either understand a Math Concept or Tool, or you don't.

And, the teacher will be going too slowly for other students and they will become bored and frustrated. Bad for them too.

Grading on the Bell Curve is a HOAX.
Math performance is essentially bi-modal.
Either you understand a math topic, or you don't.

## SPIKE Pedagogy

So, if a teacher tries to slow down as much as possible to keep slower students from failing, this then makes the Math boring for the faster students.

Also, note any student may learn one topic fast and another topic slow.

Self-pacing is critically important.
Boredom with a subject again creates bad psychology and bad ultimate results.

## Conclusion:

Deliver Math Education to your students utilizing SPIKE Pedagogy.

Struggling Students

## Chapter 4: Teacher \& Coach

To learn Math, a student needs both a teacher and a coach.

The teacher selects the appropriate topics for a student, then explains each topic, and gives the student exercises and feedback via a quiz.

The coach monitors the student's activities and gives the student motivational feedback with both "carrots" and "sticks".

The "sticks" might be requiring the student to spend a certain amount of time studying math with the teacher.

The "carrots" are giving the student positive feedback in the form of compliments and rewards for efforts and accomplishments.

Mistakes are unavoidable when learning math, just like any sport or skill.

The coach should acknowledge the student's mistakes as good efforts and progress in learning the math concepts and skills.

DO NOT ever let a student feel s/he is a "failure" because of some mistake s/he makes. Celebrate mistakes as a sign of effort and progress.

A coach should be able to come up with various "rewards" for a student's progress and efforts.

## Recognition and sincere compliments are often the best rewards.

A coach must be present in a student's life, and care about the student, and make persistent and consistent efforts to give the student these positive feedbacks.

And, a "kick" when needed.
A coach must be prepared to encourage the student to make efforts even when these efforts seem to not be producing good results.

All successful people go through periods of "doldrums".
Any successful person in the development of any skill will make many "mistakes".

## That's life! We all live it.

The coach must be sure the student understands this and appreciates this.

Compare Math to some game or sport or music or any other skill the student likes. We all make mistakes.

The more we practice, the more mistakes we make, and the better we become.

The better we become, the fewer mistakes we make, but we will always make mistakes.

The more we learn, the more mistakes we will have made.

The coach should try to help the student see where learning the concepts and skills of Math will help the student in other areas of interest to the student.

If a student is interested in any technical field $\mathrm{s} / \mathrm{he}$ must realize the value of math in this field.

The coach should be sure the student is aware of this.

## A coach does not have to be the teacher.

The coach does not have to know much math.
The coach will work with the teacher.
It is possible that one person can be both the coach and the teacher, but, this is usually impossible.

## I can be the teacher thanks to modern technologies

## You can be the coach.

Any parent must find a local person to be the coach, whether that person be the parent or another person, since this requires a continual presence and a personal relationship.

Sometimes the student can be his or her own coach.

Struggling Students

## How to Be a Great Coach

## Chapter 5: How to Be a Great Coach

## Motivation and Learning Techniques

## Motivation:

## Intrinsic vs. Extrinsic

Intrinsic Motivation . . . is when a student studies and learns math simply for the internal satisfaction and enjoyment.

It is what usually motivates a person to play a game or sport.

Once a student starts to learn math and gain confidence and self-esteem, intrinsic motivation often sets in.

This is what we want as a coach and teacher.
However, for many students this takes some time.
In the meantime, a Coach can use extrinsic motivators.
Extrinsic Motivation . . . is when a student wants something that the study of math will provide. That "something" is an extrinsic motivator.

For example, if a student wants to study any STEM subject then that is an extrinsic motivator since Math is necessary for practically any STEM subject.

If a student wants to enter any technical field in industry or the military, then practical math is necessary, and that is an extrinsic motivator.

Triad Math's Tiers 1 and 2 provide this necessary math, and also are a great foundation for future math studies.

If a student wants to excel on the SAT, then Triad Math's Tier 3 program will satisfy this need.

Of course, other extrinsic motivators can include any type of rewards.

These can include grades, praise, privileges, money, or many other things the student might want, including the avoidance of some type of punishment.

However, we find that when the proper content and SPIKE Pedagogy are utilized by the teacher, then usually the student becomes intrinsically motivated since most of us enjoy anything that is challenging and we succeed at.

Okay, let's assume that your student is motivated enough to study math.

It is imperative that the math be taught in such a way that the student is successful. Only that will lead to intrinsic motivation.

## Learning Techniques.

To successfully learn math, a coach should teach the student to engage in certain practices.

This is different than teaching the math itself.
That is why a coach and teacher are two different necessary components of a good math learning experience.

I recommend Dr. Barbara Oakley's great book, "A Mind for Numbers - How to excel at math and science, even if you Flunked Algebra" for an elaboration on what I am going to recommend to you as a coach and to any student.

First, be sure the student studies topics in a proper sequence so that the student always has the necessary prerequisite knowledge for the topic at hand.

In other words, Proper Content. Chapter 2.
Go back and fill in any deficiencies you can identify.
First, follow the Six Tiers if you utilize me as your teacher.
Do not skip any lessons, and review a lot to be sure you don't forget what you have learned.

Second, be sure the student studies a new topic with a focused approach by studying the Notes with the Tutorial Video and then working on the exercises.

Concentrate with no distractions.
Do this for a reasonable length of time until either the student understands the topic and how to do the exercises, OR until the student gets confused and tired.

15 to 30 minutes usually good for one session.
Then STOP. Take a break!
Third, have the student engage in various activities so his or her mind can go into an Unfocused Mode.

This is when and where the sub-conscious mind processes the focused activities.

We don't understand how this really works, but it often does.

Usually, this involves some routine task or habit that requires little thought.

Do some routine boring chores.
Watching entertaining videos or playing games may not work.

You want the mind relaxed.
Who knows?
Try various things and see what works for the student.
Fourth, have the student then engage in another focused session and work on the same topic.

Now, usually the topic seems more understandable and the confusion lifts some.

It's pretty amazing how often this works.
Persistence will yield success.
No one to my knowledge knows how this really works, but it does often work.

Your subconscious mind is a great mystery and miracle.
Many great thinkers have confessed this is how they often solve a problem or discover a new concept.

It certainly works for me and I use it all the time.
Try it. Give it a chance to work.

It is important for a coach to explain and convince a student that $s /$ he will succeed if $s /$ he practices and tries hard enough and perseveres.

I can remember many times when as a student I struggled with a new concept, and then after several focused and unfocused sessions, it finally fell into place.

That's how I wrote my thesis for my Ph.D. in Math.
Sometimes, after I mastered a topic I wondered why I ever had a problem with it in the first place.

Often, you have to try many things and go down many blind alleys before you achieve the understanding and solve the problem.

The more you believe in your capabilities the more success you will have.

Yes, you will have failures and frustrations.
The more difficult the problem or concept, the more you will experience this.

But, the greater the reward and satisfaction will be when you achieve the breakthrough and achieve success.

A good coach will explain these things and encourage the student.

Celebrate mistakes as progress, too.
Success does breed confidence and more success.
But, failure should also be a sign of progress in ultimately achieving success.

Success is built on the back of many failures.

A student must "learn to learn" and a coach can greatly facilitate this.

The coach and teacher must work in tandem.
Eventually, the student should become the student's own coach.

AND, the student should be able to apply the same techniques to learning other subjects, too!

Learning math will also teach a student how to "Learn to Learn" for any subject.

And, this is the key to success in life!

## Chapter 6: Grace's Story

## My journey as a struggling math student:

I started public school in kindergarten like any other American child.

However, problems started to arise as early as first grade. I was having immense issues with mathematical concepts and simply understanding the subject in general.

My first grade teacher tried her best to help me amongst her limited amount of time and the responsibility of 20 other students.

It wasn't enough.
She taught me little tricks here and there to at least get me to understand the homework, which I did find somewhat helpful.

Unfortunately, none of the concepts were ever fully mastered.

Since she didn't have much time or attention to offer me, she would buddy me up with another student, who was basically a genius for our age at the time. Like my teacher, he wasn't very helpful either.

Second grade, I am afraid, was not any more successful than first grade.

My teacher that year was less patient than the previous ones and couldn't afford to spend any time tutoring me one-on-one.

I remember crying in the bathroom in between classes because of all the red Xs on my math homework.

She would punish the whole class by taking away recess and using that time instead to help me understand the math lesson.

My classmates ended up hating me, and my extreme dislike and basically hatred for math began.

My mom took me out of public school shortly after due to horrible math grades and the teachers who could do nothing further for me.

I struggled for eight more years, trying several different math curriculums and understanding very little, which just ended up in arguments with my mom.

My attitude towards math over the years grew so poor that I would skip lessons and lie about doing math like I was supposed to.

I would hide my lack of understanding math from my friends due to extreme embarrassment.

It wasn't until my sophomore year in high school that I took the ACT and realized there might be a chance of failing it simply due to math.

In all honesty, I excelled at every other subject except math and saw my ACT grade being very low just because of my lack of mathematical understanding very upsetting.

I reached out to a counselor from my umbrella school and she told me about Triad Math.

She explained it would teach me principles I needed to know to graduate and for basic life applications.

After some research and hearing successful testimonies from other struggling students, I gave it a shot.

## My Experience with Triad Math - Success at last!

Immediately after starting the Triad Math program, I could tell this program was nothing like anything else I had done before.

The first 12 lessons were dedicated to learning the functions and proper use of a TI-30Xa Scientific Calculator, which is completely unlike any other math curriculum out there on the market.

I had the belief that calculators were not acceptable to use, and were in fact, bad. I had been taught that manually solving problems was the correct and right way instead.

Dr. Del teaches the invalidity of that belief and how the calculator is a power tool that needs to be utilized.

He goes on to teach pre-algebra, algebra, geometry, and trigonometry in short, concise, and easily understood lessons without making me feel dumb or incompetent.

I was allowed to learn at my own pace, which was so helpful, especially as someone who needs constant review and struggles with understanding mathematics in general.

I was not given any of these opportunities in public school or with any standard math curriculum I studied at home.

Triad Math has helped me since then grow in not only my knowledge of math, but also become more confident than with any other math program.

Before Triad Math, I was embarrassed, never talked about math, and avoided it at all costs.

Now, I am not immediately frightened by a math problem and have a more open and healthy attitude toward mathematical concepts.

Honestly, I do not love the subject of math, but I am more confident and feel less inferior thanks to Triad Math. Every struggling math student needs to invest in a better education with Triad Math.
-Grace Libman

## Dr. Del's comments:

Grace's story is pretty extreme since she suffered from the very beginning.

Many students do well in math for some time, and then meet a class where for some reason they struggle and "fail".

Then, they develop a fear or dislike of math.
Perhaps not as extreme as Grace's, but bad enough to cause them to cease to do well in their future math studies.

This can happen at any stage in a student's career.
The next story tells of student, Craig - me, where the student did well in math until meeting a bad class, in this case $9^{\text {th }}$ Grade in high school.

## Grace's Story

Craig's story had a "happy ending" due to two very good teachers Craig was fortunate to have.

Most students have not been so "lucky".
Thanks to modern technologies, any student today can enjoy similar "good luck" thanks to Triad Math and Craig, aka Dr. Del.

Struggling Students

## Chapter 7: Craig's Story

Delbert Craig Hane, aka Dr. Del, aka Craig Hane, Ph.D. (Math) was born in Greencastle, Indiana, on November 30, 1938.

His family moved into a small bungalow on the banks of Deer Creek, five miles south of Greencastle, in the woods.

No running water, no central heat, no phone, no TV, but they did have electric lights, a radio, a manual water well pump, and an outhouse.

The only neighbors were Craig's Uncle Jack and Aunt Inez, a short path away in a log cabin his Uncle Jack had built five years earlier.

Lots of pets and wild life of all kinds.
Life was wonderful for Craig!
Play in the creek and take long walks in the woods, and read books and listen to the radio.

Craig's parents both worked.
Dad, in a war factory in Indianapolis, and Mom, in a beauty shop in Greencastle.

Craig spent a lot of time with his Aunt Inez and Uncle Jack.

Uncle Jack was a barber and builder.
He had built his log cabin in about 1933 during the Great Depression.

Uncle Jack knew a lot of practical math needed for life and building.

He taught Craig how to count with the decimal number system using Cheerios and dimes and pennies when Craig was 4 and 5 years old.

Homeschooling!
Craig was enrolled in the first grade at age 5 in a four room school with eight grades in Putnamville, about 3 miles away, a short school bus ride.

He was the youngest student in the first grade and the least mature.

His poor teacher Miss Bernice Lewis worried since he couldn't skip, sing, or color right since he was color blind.

Dumbest kid in first grade!
Then one day she started teaching the first graders to count.

None of them had been taught to count yet.
Most couldn't get past 10.
But, thanks to Uncle Jack's homeschooling, Craig could count to 100 and beyond.

Wow!
Miss Lewis was impressed.

So, Miss Lewis had Craig help her teach his older more mature classmates how to count, and begin to add too!

This might have been the most important psychological thing to happen to Craig in his whole life.

Confidence and self-esteem!
Respect from his peers for the first time.
Craig also then learned the second grade math, too, since they were in the same room.

So by age six, Craig was well ahead of his classmates in math.

Thanks to more math from his Uncle Jack, Craig stayed at top of his class all through the $8^{\text {th }}$ Grade.

Not only good with numbers, but practical geometry a builder knows too! (See the Uncle Jack videos for parents.)

Craig's family were all working folks. His dad had an $8^{\text {th }}$ Grade education.

No one in his entire extended family had ever gone to college.

College was considered the passport to great success, and Craig was always told by his family that HE would someday go to college and have success more than any of them had achieved.

## Ooops!

A horrible set back occurred in Craig's Freshman year, $9^{\text {th }}$ Grade, in Greencastle High School.

Algebra 1! With a teacher, Mr. H.H.
Algebra was beyond anyone in Craig's family including Uncle Jack.

Even Craig's 8 ${ }^{\text {th }}$ Grade teacher wondered what "x" meant.

No help now from Homeschooling.
Craig struggled and didn't like Mr. H.H. since he couldn't understand him and get his questions answered.

And, Craig always made a lot of careless errors when taking a timed test.

The result?
A Bad Grade in Freshman Algebra.
Craig's GHS Counselor and Principal BOTH told Craig he should take "Shop" since he was not "college material" like the upper class kids and would obviously be a "working man" like his dad and family.

Wow! No college.
Craig was pretty depressed all summer before the $10^{\text {th }}$ grade.

Then, in the $10^{\text {th }}$ Grade, Craig had an amazing teacher, Miss Madonna O'Hair for Geometry.

She taught him to prove theorems logically, sort of like his Uncle Jack approached practical math.

Craig loved it and excelled and got an A.
On top again.

Then, Craig had Mr. H.H. in the $11^{\text {th }}$ Grade for Algebra 2.
Now things were different.
Craig became a very unliked student since he now asked questions and demanded logical answers that Mr. H.H. wouldn't give him.

To be fair, Mr. H.H. probably couldn't.
Bad student.
Bad grade again.
Craig went to Miss O'Hair for advice.
DePauw University is in Greencastle and only the brightest GHS graduates could go there.

Miss O'Hair suggested to Craig that he go to DePauw his senior year as a Special Student and take Algebra there and see how it went.

Mr. McCammon, the GHS Principal, strongly objected, "Craig, you'll embarrass GHS. You will not do well in Algebra since you didn't do well in Algebra twice here."

Craig's dad, Delbert, had a talk with Mr. McCammon and Craig was given permission to embarrass GHS.

So, 16 year old Craig enrolled in College Algebra at DePauw as a Special Student.

Mistake!
This was for DePauw Sophomores.
He should have been enrolled in Freshman Intemediate Algebra.

So, Craig was in a class with 19 and 20 year old DePauw students who were going on in Math.

The Professor was Dr. Clint Gass, who was the DePauw Math Department Chairman.

Long story short, Dr. Gass was a great teacher like Miss O'Hair, and Craig got an A.

Dr. Gass became Craig's mentor, too.
In the second semester Craig took Trigonometry at DePauw with Mr. Johnson and got an A there, too. Good teacher again.

In Craig's Junior year at GHS he tutored the captain of the football team, Fred U., in Geometry, and was paid to do so by Mrs. U. Wow!

Getting paid for something he loved to do. Amazing!
Then Mr. H.H. was teaching Trig to the Junior and Seniors at GHS, and Mr. H.H. got the flu.

Miss O'Hair was asked to teach the class for a week.
She said she would only do so IF Craig could teach it.
After all, he was learning Trig at DePauw and was a couple of weeks ahead of GHS.

So Craig got his first experience teaching a whole class.
The topics were Trig Identities and all the GHS students learned them in the following week.

When he returned Mr. H.H. told the class Identities were not important and there would be no test!

Mr. H.H. was probably a typical H.S. math teacher, incompetent.

Miss O'Hair was an exception.
Craig was extremely lucky or fortunate to first be homeschooled by Uncle Jack, than a wonderful good teacher Miss O'Hair, and then a wonderful college professor, Dr. Gass.

Craig had a mediocre GPA in high school.
He worked about 20 hours per week from $7^{\text {th }}$ Grade on, and saved all his money. No time for wasting it anyway.

By the end of his senior year, Craig had enough money for four years tuition at a private school like DePauw.

But, Craig wanted to escape Greencastle and go to a College like DePauw, but with no Greek fraternities and sororities.

Oberlin College was a few hours away on the Pennsylvania Railroad, and Craig visited and loved it. So, he applied.

Craig was accepted to Oberlin College, the No. 1 Liberal Arts College in the USA in 1956 thanks to the huge endowment by Charles R. Hall who founded Alcoa.

Craig believes this was due to Dr. Gass's recommendation.
Craig now had self-confidence in math and did well at Oberlin.

He also taught math to his classmates as a paid Problem Session Instructor. He used what is now called SPIKE Pedagogy.

Then, upon graduation in 1960, he taught all four classes of Math for one year on a temporary license at Western Reserve High School in Wakeman, Ohio, 20 miles west of Oberlin.

That was the most wonderful year as a teacher in Craig's life.

And, he fully came to believe that Math Education in most of the USA was truly horrible.

Most of his successful fellow Math Majors at Oberlin had been to private schools or wonderful public schools in New York or some other large city.

Graduates of ordinary high schools had little chance for success in math.

Craig believed he had just been incredibly lucky to have Miss O'Hair and then Dr. Gass as teachers.

Home for the summer and visiting Dr. Gass as usual, Dr. Gass invited Craig to teach Math at DePauw the second semester in 1962, while he, Dr. Gass, went on sabbatical.

Dr. Gass also suggested that Craig enroll in graduate school math at Indiana University to see what it was like.

Craig did both, and then received his Ph.D. in Theoretical Math from I.U. in 1966.

Just imagine.
"You are not college material due to your Freshman Algebra 'failure'" in 1952 at GHS to teaching Math at DePauw in 1962.

Then, getting a Ph.D. in Math at Indiana University in 1966, and on to Associate Professor of Math at Indiana State University teaching the most advanced math subjects for three years.

Then, Associate Professor of Math at Rose Hulman Institute of Technology teaching the most advanced math subjects like Topology and Functional Analysis, for four more years.

Then, Craig decided to have several business adventures, one of which was to found an industrial training company in 1980, which taught thousands of skilled tradesman technical subjects for 25 years.

Visit: www.HaneTraining.com to see them.
Craig always wanted to see Math Education reformed, but had no practical way to help do this until $21^{\text {st }}$ Century Technologies appeared.

In 2008, Craig began to create a modern $21^{\text {st }}$ Century Math Program and was amazed when in 2009 Wolfram Alpha arrived on the scene.

The rest is history.
In the next Chapter you can learn about the Six Tier Math Program Craig created that is the first $21^{\text {st }}$ Century Math Program to appear.

It is Vastly Superior to the current Standard Math Curriculum Programs in both Proper Content and SPIKE Pedagogy.

Be sure to try one of the Special Offers to prove it to yourself and your children, like Grace Libman, and many others have.

Nothing to lose, and much to gain!

## Chapter 8: Future Math Possibilities

## Tiers 1 - 6 Syllabus Overview

For full details go to: www.CraigHane.com and you may download the full syllabus about half way down my home page.

## Getting Started. Tier 1 and the Scientific Calculator

Tier 1 teaches the student how to use a scientific calculator, the TI-30Xa: 16 Lessons.

Then, PreAlgebra, which is a review of the Rules of Arithmetic. 10 Lessons

Tier 1 usually gets any student into a good frame of mind and convinces them Math can be easy and fun.

Getting a student's psychology set regarding Math is the first and most important thing to do. See Chapter 5.

## Foundation - Practical Math. Tier 2

Tier 2 covers Practical Algebra (10 Lessons), Practical Geometry (19 Lessons), and Practical Trigonometry (7 Lessons).

Most students can cover this in about 60 hours of study time $+/-30$ hours, depending on their background and their math aptitude. So, about one semester.

Now, a student is really confident of their ability, and most now really like math.

They also realize that they are now prepared to learn many different technical subjects.

Indeed, they will now know more math than $95 \%$ of adults in the USA.

They are ready for the military and apprentice programs.
They have high confidence and self-esteem.
Here's a problem they will be able to solve in less than one minute. You, the reader, can try it or give it to someone you know.

Find the area of a triangle whose sides measure $6.4 \mathrm{ft}, 8.7 \mathrm{ft}$, and 12.3 ft

Answer: 26.5 sq ft

## College-Bound SAT or ACT Prep. Tier 3

Some of these topics are good for Consumer Math.
Some of these topics are good for Quantitative Reasoning.
Some of these topics are just good for tricky questions on a test like the SAT.

Most students take about a year to master Tier 3.
Part 1 of Tier 3 should prepare you for a standard test you will need to pass to graduate from high school.

Part 2 of Tier 3 will teach you additional mathematics you will need to excel on the SAT and ACT and other exams.

Part 3 is SAT Prep, how to prepare and how to take such an exam.

Ok, this will help you get into college by scoring higher on the SAT or ACT tests.

But, will it mean you are prepared for a STEM subject in college?

No.
You will need a lot more math to be well prepared for a STEM subject and to compete with other students who have been properly educated with STEM Math.

## STEM Math PreCalculus. Tier 4

Now, we will cover Algebra, Geometry and Trigonometry at a much deeper level required for STEM, plus much more!

We now introduce and use a $21^{\text {st }}$ Century Math Tool unleashed on the world in 2009: Wolfram Alpha.

Wolfram Alpha revolutionizes the way you learn math and do math, i.e. solve Math Problems.

No math textbooks teach this as far as I know, as of July 2021.

No math courses in any schools teach this either, so far as I know.

In Tier 4, we also teach Complex Numbers the proper way by utilizing Euler's Equation and the Geometric Approach which unites Complex Numbers with Trigonometry.

Again, I know of no current math curriculum that does this.

AND, it is vitally important for many STEM subjects in Science and Engineering.

## Calculus the right 21st Century way. Tier 5

Differential Calculus, Calculus 1, teaches a student how to analyze functions, which are the building blocks of all STEM subjects.

This is not too difficult with the old manual tools, but time consuming and error prone, and often not possible for some problems.

With Wolfram Alpha, it is now very easy and will solve any calculus problem.

Integral Calculus, Calculus 2, is very difficult when using the old manual tools.

One must find the anti-derivative of a function to apply the Fundamental Theorem of Calculus to calculate a definite integral.

Finding the anti-derivative can be very difficult and timeconsuming, and often impossible with ordinary functions.

Calculus 2 probably has flunked more students out of STEM schools than anything else. Some schools use it as a "filter" to "weed out" weak students, but ironically, it often weeds out very good students, too, who have just had some poor teachers. I can tell you some horror stories.

Now, Wolfram Alpha makes Integral Calculus very easy, too. It will find the anti-derivative of any function, even if it involves a Special Function.

Now, Calculus goes from an 8 on the difficulty scale of 1 to 10 down to a 2.

And, it gets even better.

Now, most students can learn Calculus in Tier 5 in about one semester, not one or two years like the old manual Calculus.

And, the student will now be ready to compete with their best-trained peer students.

## Differential Equations. Tier 6

Differential Equations are the workhorse of Science and Engineering subjects.

Historically, Differential Equations are not taught in high school because they are too difficult.

Most schools don't even teach Integral Calculus.
Solving Differential Equations whose solutions are functions is even more difficult that Integral Calculus.

All changed in the $21^{\text {st }}$ Century due to what ??????
Wolfram Alpha.
In Tier 6, we teach a student how to solve Differential Equations with Wolfram Alpha.

This takes most students about one semester.
SO, today if a student starts studying our Program at say age 12, the student should get through Tier 6 by age 16 or 17.

Also, the student will probably acquire a SupraComputer and begin to learn Wolfram Language which was introduced to the world in 2016.

Now, the student is off to the STEM races.
Homeschools, private schools, and charter schools will probably lead the way.

They can now use an online program utilizing coaches to teach $21^{\text {st }}$ Century Math the right way, thanks to many new technologies.

Amazingly, sometimes a Struggling Student goes on to study STEM subjects after getting turned around, like I did.

I recommend you read my book, Golden Rule Math for STEM Students where there is a more in depth discussion.

## Free Resources

Simply go to www.CraigHane.com to get the current free resources available from Dr. Del.

The Video Library Tab will yield many videos Dr. Del has created, and is an ever expanding Library.

These videos are all Youtube videos.
Potential STEM students will want to watch the three videos on the Concepts of Calculus.

Some are also Youtube videos of others that Dr. Del finds inspirational and informative.

Struggling Students

## Special Offers

Go to www.TriadMathInc.com/SO for the current Special Offers.

> Dr. Del and Triad Math, Inc. like to give students and families actual training so they can evaluate the methods our Programs use to determine if they would then benefit from some of our training products.

Seeing is believing.
Your experience is the only one that counts for you.
So, go take advantage of our current Special Offers.
Dr. Del wants the best for you and your family.

Struggling Students

## Affiliates

Go to: https://www.triadmathinc.com/affiliate/
to learn about our current Affiliate Program.
The Affiliate Program is designed to empower you to help other students and families improve their lives.

Usually, this will involve giving them a valuable gift from Triad Math with your recommendation to try it.

Giving your own testimonial experience will be invaluable in getting them to use the gift.

Then, IF they purchase a product from Triad Math, Inc. you may be eligible for a commission or some other valuable product.

Dr. Del's Mission should be one you share, which is to help student's get an Optimal Math Education in the best way possible.

Struggling Students

## Who is Dr. Del?

Dr. Del is a pen name used by Delbert Craig Hane, Ph.D.
You may get a full biography at: https://craighane.com/vita-of-craig-hane-ph-d/
or just go to www.craighane.com and press the Vita Tab.
In a nutshell, Dr. Del has been a Learner of Math and a Teacher of Math for over 75 years.

75 years?
Yes. Craig was taught the decimal number system and how to count and add by his Uncle Jack (Davis) who was a barber and builder, using Cheerios in about 1942-3 when Craig was five years old.

This was the beginning of WWII for the USA and most parents were heavily involved and had little time to teach their children at home.

When Craig was five years old he was enrolled in the first grade at Putnamville, Indiana, a four room school with eight grades.

He was the youngest student in the first grade with teacher Miss Bernice Lewis.

Craig also was the only student in this first grade who had been taught to count in the decimal number system and so

Miss Lewis had him help her teach his classmates to count.

Thus, Craig had his first teaching experience at age five.
No doubt this was a life transforming experience.
You are urged to have your children teach other children things they have learned as soon as possible to other children.

Of course, Craig went on to learn math from other teachers and teach other students math the rest of his life right up to the first writing of this book, July, 2021.

Learning and teaching math are just two sides of the same coin.

Then, applying math to all sorts of situations in the real world can lead to all sorts of wonderful successes.

